35 Elementary Chemical Kinetics

Chemical reactions: Reactants→Products

Essential treaties:

- ► Reaction rate and method to determine the reaction rate
- ► Concept of reaction mechanism in terms of elementary reaction

Elementary reaction

A+B→Product

Reaction rate

$$Rate = -\frac{dn_A}{dt} = -\frac{dn_B}{dt} = k n_A^1 n_B^1$$

Rate of reaction is proportional the concentration (=Mass action)

Elementary reaction is described by

- ►Integrated rate law and
- ►Numerical method (when integration is not possible)

35.1 Introduction to Kinetics

- ► Transport phenomena: Chemical composition is not changed.
- ► Thermodynamics:
- -Spontaneity determined by $\Delta G < 0$
- -Equilibrium composition of reactant and product determined by K
- ►Kinetics:
- -How fast the reaction proceed?
- -Time scale is described.
- -Determine the rate of concentration change

(See Figure 1) in terms of temperature, pressure, concentration \rightarrow Elucidate the reaction mechanism



FIGURE 35.1

Concentration as a function of time for the conversion of reactant A into product B. The concentration of A at t = 0 is [A]₀, and the concentration of B is zero. As the reaction proceeds, the loss of A results in the production of B.

Figure 1

35.2 Reaction rate

$$aA + bB \dots \to cC + dD + \dots \tag{1}$$

A, B....= Chemical speciesLHS=Reactants, RHS=Productsa, b.. = Stoichiometric coefficient

Number of moles of a species i at any time is given by:

 $n_i = n_i^o + \nu_i \xi \tag{2}$

 $n_i = Nmberof moles of species \ i \ at \ time \ t$ $n_i^o = Nmberof moles of species \ i \ at \ time \ t = 0$
$$\begin{split} \xi &= Advancement \ of \ reaction \ (Extent \ of \ reaction) \\ &= 0 \ at \ t = 0 \\ \nu_i < 0 \ for \ reactant, \ > 0 \ for \ product \end{split}$$

Change of moles of reactants and products are given by:

$$\frac{dn_i}{dt} = \nu_i \frac{d\xi}{dt} \tag{3}$$

Reaction rate is defined by

$$Rate = \frac{d\xi}{dt} \tag{4}$$

Then the rate of reaction wrt the change of moles of species, i

$$Rate = \frac{1}{\nu_i} \frac{dn_i}{dt} \tag{5}$$

Example

$$4NO_2(g) + O_2(g) \to 2N_2O_5(g)$$
(6)

$$Rate = -\frac{1}{4} \frac{dn_{NO_2}}{dt} = -\frac{dn_{O_2}}{dt} = \frac{1}{2} \frac{dn_{N_2O_5}}{dt}$$
(7)

See the sign convention for reactant and product.

- ► Rate of conversion of NO_2 is four times of O_2 .
- "Rate" is positive, even though the moles of reactant decreases w/ time, according to the sign convention!
- ► Rate as written is an extensive property since it depends on the system size (More n_{O_2} increases rate).
- ►Rate becomes intensive property by dividing (5) by the system volume:

$$R = \frac{Rate}{V} = \frac{1}{V} (\frac{1}{\nu_i} \frac{dn_i}{dt}) = (\frac{1}{\nu_i} \frac{d(n_i/V)}{dt}) = \frac{1}{\nu_i} \frac{dM_i}{dt} = \frac{1}{\nu_i} \frac{d[i]}{dt} \quad (8)$$

$$M_i = \frac{moles \ of \ i}{\ell \ of \ solution} = Molarity$$

$$(Note \ m_i = \frac{moles \ of \ i}{kg \ of \ solvent} = Molality)$$

NOTE

- ►R is an intensive property.
- ► Moles of species i per unit volume = molarity (M=moles/L)
- $\rightarrow R$ has unit of M/t
- ► Eq (8) is the definition of rate of reaction at constant volume (Solution reaction).
- ►But it can also be used for gases as EXAMPLE 35.1.

EXAMPLE PROBLEM 35.1

The decomposition of acetaldehyde is given by the following balanced reaction:

$$CH_3COH(g) \rightarrow CH_4(g) + CO(g)$$

Define the rate of reaction with respect to the pressure of the reactant.

Solution

Beginning with Equation (35.2) and focus in on the acetaldehyde reactant, we obtain

$$n_{CH_3COH} = n_{CH_3COH}^o - \xi$$

Using the ideal gas law, the pressure of acetaldehyde is expressed as

$$P_{CH_3COH} = \frac{n_{CH_3COH}}{V} RT = [CH_3COH]RT$$

Therefore, the pressure is related to the concentration by the quantity RT. Substituting this result into Equation (35.8) with $\nu_i = -1$ yields

$$R = \frac{Rate}{V} = +\frac{1}{\nu_{CH_3COH}} \frac{d[CH_3COH]}{dt} = \frac{1}{-1} \frac{d[CH_3COH]}{dt}$$
$$= -\frac{1}{RT} \frac{dP_{CH_3COH}}{dt}$$

35.3 Rate Laws

Rate of reaction=f(T, P, Concentration) Homogeneous reaction (single phase reaction) vs heterogeneous reaction (Reactions on catalyst surface)

Rate law=Empirical:

Homogeneous reactions are treated in this chapter: For the reaction (1) (Irreversible)

$$aA + bB \dots \rightarrow cC + dD + \dots \qquad (1)$$

 $R = k[A]^{\alpha}[B]^{\beta}..... \tag{9}$

 $\begin{aligned} k &= Reaction \ rate \ constant = f \ (T) \ but \ independent \ of \ concentration \\ [A], \ [B]..... &= Concentration of A, B... \\ \alpha &= reaction \ order \ wrt \ A, \quad \beta &= Reaction \ order \ wrt \ B \\ \alpha &+ \beta..... &= Overall \ reaction \ order \\ \alpha, \beta..... Determined \ by \ experiment \\ If \ \alpha &= a \ and \ \beta &= b \ \longrightarrow \ Called \ non-elementary \ reaction \\ If \ \alpha &\neq a \ and \ \beta &\neq b \ \longrightarrow \ Called \ non-elementary \ reaction \end{aligned}$

Example

 $4NO_2(g) + O_2(g) \rightarrow 2N_2O_2(g)$